Recall: A basis of vector space V 13 any subset BEV such that OB is lin. ind. @ B spens V. "The only lin cont. girty Or X is the Zero-continuture" "Every vector in V is a linear comb. of " V vectors from B" Prop: B is a basis of V iff every vector of V arises as a unique lin. Lomb of elts from B. Recall: din (V) = number of elements in a basic for V. Exi R" his divensm n: E= {e,,e,,,,,} Recall: L: V-sW is linear when for all u,v & V and all CETR we have L(u+c·v) = L(u)+c·L(v).

NB: easiest condition to check... The rank of L is dim (ran (L)).
The nullity of L is dim (ker (L)). -) range of L is ran(L) = { L(v) : v ∈ V} Lyin, set of outputs of function L A Kernel of L is ker(L) = {v ∈ V : L(v) = Ow}
Lie. Set of vectors mapping to Or under L. Rank-Nullity Formula: dim (dam (L)) = rank(L) + nullify (L). [x: D = {(i),(i),(i)}. Show D is dependent. Method: a(i) + b(i) + c(i) = (i)

$$\begin{cases} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} \frac{1}{0} \\ \frac{1}{0} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 \\$$

$$= \{(a-c)V_1 + (b+c)V_2 : a,b, \in \mathbb{R} \}$$

$$= \{(aV_1 + \beta V_2 : K, \beta \in \mathbb{R} \}.$$

$$Span(D) = Span(D) \{v_3\}$$

$$A(\frac{1}{0}) + b(\frac{0}{1}) + c(\frac{1}{0}) = \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

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$$A(\frac{1}{0}) + c(\frac{1}{0}) + c(\frac{1}$$

$$E_{x}: I_{s} S = \{(0, 0), (0, 0), (0, 0), (0, 0)\} \}_{x}, 7$$

$$Sol: x(0, 0) + y(0, 0) + z(0, 0) + w(0, 0) = (0, 0)$$

iff
$$\begin{pmatrix} x+y \\ z+v \end{pmatrix} = \begin{pmatrix} x+y \\ z+v \end{pmatrix} = \begin{pmatrix} x+y \\ y+z \\ z+v = 0 \end{pmatrix}$$

so solve system: $\begin{pmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \end{pmatrix}$

show this has only 0 -solution, so they're LI. In the solution of the second of the solution of the second of the second

To compte a besis for range: $ran(L) \stackrel{!}{=} \left\{ L(v) : V \in dom(L) \right\}$ $\stackrel{!}{=} \left\{ L(a+bx+cx^2+dx^3) : a,b,c,d \in \mathbb{R} \right\}$

is by Rack-nullity frank: 4= 1+ rank(L)

in vark (L) = 3.